



Statistical „Pole Position” Leadership between Lamborghini versus Ferrari

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ABSTRACT

Lamborghini and Ferrari represents two great hyper powers in the worldwide sphere of the firms which product cars of high performance. In each year, the both firms highlight new models cars at the great salons of expositions, where the prototypes innovated fascinate through shapes, horsepower, engine systems, top speed, electrical performances and more indexes which reflect the „implant” concerning the management of the quality.

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1. Introduction

This statistical highlight puts in evidence the competition between two great firms which conquered the lovers of performant cars, namely Lamborghini and Ferrari. The target of this research follows the achievement of the forecasts concerning the values of the levels touched in the sales of vehicles by the both firms, Lamborghini and Ferrari, for to reflect the real leadership highlighted in „pole positions”. The first side of this statistical research brings in first plane, how we can to select the trend concerning the number of Lamborghini vehicles sold between 2006-2018, at the worldwide level. The second side guides the readers in the achievement of the methodology regarding the selection of the model which reflects the volum of Ferrari vehicles merchandised in all over the world, in the same interval 2006-2018. The methods used are the „Regression Method” and the „Variation Method” for to achieve the forecasts regarding the values of Lamborghini and Ferrari vehicles sold at the worldwide level. In 1823, Johann Carl Friedrich Gauss drewed up the „Least Squares Method”, where the target is the identification of the parameters which belong to the model puts in the sphere of the research.

2. The design of the projection concerning the volum of the worldwide sales for the Lamborghini cars, between 2006-2018

Table 1 The values which have as essence the „fizzy” architectures of the both champions Lamborghini&Ferrari concerning the series of successes in the worldwide sales for vehicles

YEARS	LAMBORGHINI WORLDWIDE NUMBER OF VEHICLES	FERRARI WORLDWIDE NUMBER OF VEHICLES
2006	2087	5671
2007	2406	6465
2008	2430	6587
2009	1515	6250
2010	1302	6461
2011	1602	7001
2012	2083	7318
2013	2121	6922
2014	2530	7255
2015	3245	7664
2016	3457	8014
2017	3815	8398
2018	5750	9251

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- if the „sophisticated design” for ξ variable, namely the Lamborghini worldwide sales, is this representation $\xi_{t_i} = a + b \cdot t_i$, a and b will be [3]:

$$S = \sum_{i=1}^n (\xi_i - \xi_{ii})^2 = \min \Leftrightarrow S = \sum_{i=1}^n (\xi_i - a - bt_i)^2 = \min$$

$$\begin{cases} \frac{\partial S}{\partial a} = 0 \\ \frac{\partial S}{\partial b} = 0 \end{cases} \Rightarrow \begin{cases} 2 \sum_{i=1}^n (\xi_i - a - bt_i)(-1) = 0 / (-\frac{1}{2}) \\ 2 \sum_{i=1}^n (\xi_i - a - bt_i)(-t_i) = 0 / (-\frac{1}{2}) \end{cases} \Rightarrow \begin{cases} na + b \sum_{i=1}^n t_i = \sum_{i=1}^n \xi_i \\ a \sum_{i=1}^n t_i + b \sum_{i=1}^n t_i^2 = \sum_{i=1}^n \xi_i t_i \end{cases} \Rightarrow$$

$$a = \frac{\begin{vmatrix} \sum_{i=1}^n \xi_i & \sum_{i=1}^n t_i \\ \sum_{i=1}^n \xi_i t_i & \sum_{i=1}^n t_i^2 \end{vmatrix}}{\begin{vmatrix} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{vmatrix}} = \frac{\sum_{i=1}^n \xi_i \sum_{i=1}^n t_i^2 - \sum_{i=1}^n \xi_i t_i \sum_{i=1}^n t_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2} \quad b = \frac{\begin{vmatrix} n & \sum_{i=1}^n x_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n \xi_i t_i \end{vmatrix}}{\begin{vmatrix} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{vmatrix}} = \frac{n \sum_{i=1}^n \xi_i t_i - \sum_{i=1}^n t_i \sum_{i=1}^n \xi_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2}$$

Table 2 The „conglomerate” of the values which joins under the incidence of the reflection concerning the linear pattern for the volum of Lamborghini cars sold at worldwide level

YEARS	LAMBORGHINI WORLDWIDE NUMBER OF VEHICLES (ξ)	LINEAR TENDENCY				
		t_i	t_i^2	$t_i \xi_i$	$\xi_{t_i} = a + bt_i$	$ \xi_i - \xi_{t_i} $
2006	2087	-6	36	-12522	1280,362638	807
2007	2406	-5	25	-12030	1507,263737	899
2008	2430	-4	16	-9720	1734,164835	696
2009	1515	-3	9	-4545	1961,065934	446
2010	1302	-2	4	-2604	2187,967033	886
2011	1602	-1	1	-1602	2414,868132	813
2012	2083	0	0	0	2641,769231	559
2013	2121	1	1	2121	2868,670330	748
2014	2530	2	4	5060	3095,571429	566
2015	3245	3	9	9735	3322,472528	77
2016	3457	4	16	13828	3549,373627	92
2017	3815	5	25	19075	3776,274726	39
2018	5750	6	36	34500	4003,175824	1747
TOTAL	34343		182	41296	34343	8375

$$a = \frac{34343 \cdot 182 - 41296 \cdot 0}{13 \cdot 182 - 0^2} = 2641,769231$$

$$b = \frac{13 \cdot 41296 - 34343 \cdot 0}{13 \cdot 182 - 0^2} = 226,9010989$$

$$v_I = \left[\frac{\sum_{i=-m}^m |\xi_i - \xi_i^I|}{n} : \frac{\sum_{i=-m}^m x_i}{n} \right] \cdot 100 = \frac{\sum_{i=-m}^m |\xi_i - \xi_i^I|}{\sum_{i=-m}^m \xi_i} \cdot 100 = \frac{8375}{34343} \cdot 100 = 24,386\%$$

- if the „sophisticated design” for ξ variable, namely the Lamborghini worldwide sales, is this representation $\xi_{t_i} = a + b \cdot t_i + ct_i^2$, a and b will be [3]:

$$S = \sum_{i=1}^n (\xi_i - x_{ti})^2 = \min \Leftrightarrow S = \sum_{i=1}^n (\xi_i - a - bt_i - ct_i^2)^2 = \min$$

$$\begin{cases} \frac{\partial S}{\partial a} = 0 \\ \frac{\partial S}{\partial b} = 0 \\ \frac{\partial S}{\partial c} = 0 \end{cases} \Rightarrow \begin{cases} 2 \sum_{i=1}^n (\xi_i - a - bt_i - ct_i^2)(-1) = 0 / (-\frac{1}{2}) \\ 2 \sum_{i=1}^n (\xi_i - a - bt_i - ct_i^2)(-t_i) = 0 / (-\frac{1}{2}) \\ 2 \sum_{i=1}^n (\xi_i - a - bt_i - ct_i^2)(-t_i^2) = 0 / (-\frac{1}{2}) \end{cases} \Rightarrow$$

$$\begin{cases} n \cdot a + b \sum_{i=1}^n t_i + c \sum_{i=1}^n t_i^2 = \sum_{i=1}^n \xi_i \\ a \sum_{i=1}^n t_i + b \cdot \sum_{i=1}^n t_i^2 + c \sum_{i=1}^n t_i^3 = \sum_{i=1}^n t_i \cdot \xi_i \\ a \cdot \sum_{i=1}^n t_i^2 + b \sum_{i=1}^n t_i^3 + c \sum_{i=1}^n t_i^4 = \sum_{i=1}^n t_i^2 \cdot \xi_i \end{cases}$$

$$a = \frac{\sum_{i=1}^n t_i^4 \sum_{i=1}^n \xi_i - \sum_{i=1}^n t_i^2 \sum_{i=1}^n t_i^2 \cdot \xi_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2} ; \quad b = \frac{\sum_{i=1}^n \xi_i t_i}{\sum_{i=1}^n t_i^2} ; \quad c = \frac{n \cdot \sum_{i=1}^n t_i^2 \cdot \xi_i - \sum_{i=1}^n t_i^2 \cdot \sum_{i=1}^n \xi_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2}$$

Table 3 The „conglomerate” of the values which joins under the incidence of the reflection concerning the quadratic pattern for the volum of Lamborghini cars sold at worldwide level

YEARS	LAMBORGHINI WORLDWIDE NUMBER OF VEHICLES (ξ)	PARABOLIC TENDENCY					
		t_i	t_i^2	t_i^4	$t_i^2 \xi_i$	$\xi_{t_i} = a + bt_i + ct_i^2$	$ \xi_i - \xi_{t_i} $
2006	2087	-6	36	1296	75132	2521,43956	434
2007	2406	-5	25	625	60150	2127,802198	278
2008	2430	-4	16	256	38880	1846,990010	583
2009	1515	-3	9	81	13635	1679,002997	164
2010	1302	-2	4	16	5208	1623,841159	322
2011	1602	-1	1	1	1602	1681,504496	79
2012	2083	0	0	0	0	1851,993007	231
2013	2121	1	1	1	2121	2135,306693	14
2014	2530	2	4	16	10120	2531,445554	1
2015	3245	3	9	81	29205	3040,409590	205
2016	3457	4	16	256	55312	3662,198801	205
2017	3815	5	25	625	95375	4396,813187	582
2018	5750	6	36	1296	207000	5244,252747	506
TOTAL	34343		182	4550	593740	34343	3604

$$a = \frac{\sum_{i=1}^n t_i^4 \sum_{i=1}^n \xi_i - \sum_{i=1}^n t_i^2 \sum_{i=1}^n t_i^2 \cdot \xi_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2} = \frac{4550 \cdot 34343 - 182 \cdot 593740}{13 \cdot 4550 - 182^2} = 185,993007$$

$$b = \frac{\sum_{i=1}^n \xi_i t_i}{\sum_{i=1}^n t_i^2} = \frac{41296}{182} = 226,9010989$$

$$c = \frac{n \cdot \sum_{i=1}^n t_i^2 \cdot \xi_i - \sum_{i=1}^n t_i^2 \cdot \sum_{i=1}^n \xi_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2} = \frac{13 \cdot 593740 - 182 \cdot 34343}{13 \cdot 4550 - 182^2} = 56,41258741$$

$$v_{II} = \left[\frac{\sum_{i=-m}^m |\xi_i - \xi_{t_i}^{II}|}{n} : \frac{\sum_{i=-m}^m x_i}{n} \right] \cdot 100 = \frac{\sum_{i=-m}^m |\xi_i - \xi_{t_i}^{II}|}{\sum_{i=-m}^m \xi_i} \cdot 100 = \frac{3604}{34343} \cdot 100 = 10,49\%$$

- if the „sophisticated design” for ξ variable, namely the Lamborghini worldwide sales, is this representation $\xi_{t_i} = ab^{t_i}$, a and b will be [3]:

$$S = \sum_{i=1}^n (\lg \xi_i - \lg \xi_{t_i})^2 = \min \Leftrightarrow S = \sum_{i=1}^n (\lg \xi_i - \lg a - t_i \lg b)^2 = \min$$

$$\begin{cases} \frac{\partial S}{\partial \lg a} = 0 \\ \frac{\partial S}{\partial \lg b} = 0 \end{cases} \Rightarrow \begin{cases} 2 \sum_{i=1}^n (\lg \xi_i - \lg a - t_i \lg b)(-1) = 0 / (-\frac{1}{2}) \\ 2 \sum_{i=1}^n (\lg \xi_i - \lg a - t_i \lg b)(-t_i) = 0 / (-\frac{1}{2}) \end{cases} \Rightarrow$$

$$\begin{cases} n \cdot \lg a + \lg b \cdot \sum_{i=1}^n t_i = \sum_{i=1}^n \lg \xi_i \\ \lg a \sum_{i=1}^n t_i + \lg b \cdot \sum_{i=1}^n t_i^2 = \sum_{i=1}^n t_i \cdot \lg \xi_i \end{cases}$$

$$\lg a = \frac{\begin{vmatrix} \sum_{i=1}^n \lg \xi_i & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i \lg \xi_i & \sum_{i=1}^n t_i^2 \end{vmatrix}}{\begin{vmatrix} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{vmatrix}} = \frac{\sum_{i=1}^n \lg \xi_i \sum_{i=1}^n t_i^2 - \sum_{i=1}^n t_i \lg \xi_i \sum_{i=1}^n t_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2}$$

$$\lg b = \frac{\left| \begin{array}{cc} n & \sum_{i=1}^n \lg \xi_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i \lg \xi_i \end{array} \right|}{\left| \begin{array}{cc} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{array} \right|} = \frac{n \cdot \sum_{i=1}^n t_i \lg \xi_i - \sum_{i=1}^n \lg \xi_i \sum_{i=1}^n t_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2}$$

Table 4 The „conglomerate” of the values which joins under the incidence of the reflection concerning the exponential pattern for the volum of Lamborghini cars solded at worldwide level

YEARS	LAMBORGHINI WORLDWIDE NUMBER OF VEHICLES (ξ_i)	EXPONENTIAL TENDENCY				
		$\lg \xi_i$	$t_i \lg \xi_i$	$\lg \xi_{t_i} =$ $= \lg a + t_i \lg b$	$\xi_{t_i} = ab^{t_i}$	$ \xi_i - \xi_{t_i} $
2006	2087	3,319522449	-19,91713469	3,190572898	1550,861083	536
2007	2406	3,381295623	-16,90647812	3,223240715	1672,017101	734
2008	2430	3,385606274	-13,54242509	3,255908532	1802,638042	627
2009	1515	3,180412633	-9,541237899	3,288576349	1943,463323	428
2010	1302	3,114610984	-6,229221968	3,321244166	2095,290124	793
2011	1602	3,204662512	-3,204662512	3,353911983	2258,977904	657
2012	2083	3,318689270	0	3,386579800	2435,453264	352
2013	2121	3,326540669	3,326540669	3,419247617	2625,715192	505
2014	2530	3,403120521	6,806241042	3,451915434	2830,84072	301
2015	3245	3,511214701	10,5336441	3,484583251	3051,991017	193
2016	3457	3,538699380	14,15479752	3,517251068	3290,417968	167
2017	3815	3,581494542	17,90747271	3,549918885	3547,471254	268
2018	5750	3,759667845	22,55800707	3,582586702	3824,606000	1926
TOTAL	34343	44,0255374	5,945542830			7487

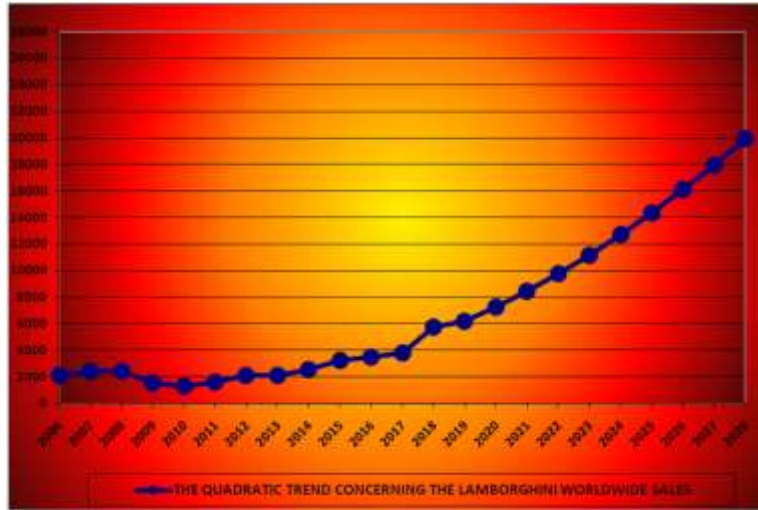
$$\lg a = \frac{44,0255374 \cdot 182 - 5,94554283 \cdot 0}{13 \cdot 182 - 0^2} = 3,3865798$$

$$\lg b = \frac{13 \cdot 5,94554283 - 44,0255374 \cdot 0}{13 \cdot 182 - 0^2} = 0,032667817$$

$$v_{\exp} = \left[\frac{\sum_{i=-m}^m |\xi_i - \xi_{t_i}^{\exp}|}{n} : \frac{\sum_{i=-m}^m x_i}{n} \right] \cdot 100 = \frac{\sum_{i=-m}^m |\xi_i - \xi_{t_i}^{\exp}|}{\sum_{i=-m}^m \xi_i} \cdot 100 = \frac{7487}{34343} \cdot 100 = 21,81\%$$

$$v_{II} = 10,49\% < v_{\exp} = 21,81\% < v_I = 24,386\%$$

The „design of the rally” regarding the projection which belongs to the Lamborghini worldwide sales, reveals a quadratic pattern $\xi_{t_i} = a + b \cdot t_i + ct_i^2$



Graph 1 The design of the quadratic pattern concerning the worldwide sales for the Lamborghini cars

. The design of the projection regarding the worldwide sales for the Ferrari cars, between 2006-2018

- if the „sophisticated design” for ω characteristic, namely the Ferrari worldwide sales, is this mirroring $\omega_i = a + b \cdot t_i$, a and b will be [3]:

$$S = \sum_{i=1}^n (\omega_i - \omega_{ii})^2 = \min \Leftrightarrow S = \sum_{i=1}^n (\omega_i - a - bt_i)^2 = \min$$

$$\begin{cases} \frac{\partial S}{\partial a} = 0 \\ \frac{\partial S}{\partial b} = 0 \end{cases} \Rightarrow \begin{cases} 2 \sum_{i=1}^n (\omega_i - a - bt_i)(-1) = 0 / (-\frac{1}{2}) \\ 2 \sum_{i=1}^n (\omega_i - a - bt_i)(-t_i) = 0 / (-\frac{1}{2}) \end{cases} \Rightarrow \begin{cases} na + b \sum_{i=1}^n t_i = \sum_{i=1}^n \omega_i \\ a \sum_{i=1}^n t_i + b \sum_{i=1}^n t_i^2 = \sum_{i=1}^n \omega_i t_i \end{cases} \Rightarrow$$

$$a = \frac{\begin{vmatrix} \sum_{i=1}^n \omega_i & \sum_{i=1}^n t_i \\ \sum_{i=1}^n \omega_i t_i & \sum_{i=1}^n t_i^2 \end{vmatrix}}{\begin{vmatrix} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{vmatrix}} = \frac{\sum_{i=1}^n \omega_i \sum_{i=1}^n t_i^2 - \sum_{i=1}^n \omega_i t_i \sum_{i=1}^n t_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2} \quad b = \frac{\begin{vmatrix} n & \sum_{i=1}^n \omega_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n \omega_i t_i \end{vmatrix}}{\begin{vmatrix} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{vmatrix}} = \frac{n \sum_{i=1}^n \omega_i t_i - \sum_{i=1}^n t_i \sum_{i=1}^n \omega_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2}$$

Table 5 The „conglomerate” of the statistical data which joins under the incidence of the reflection concerning the linear pattern for the volum of Ferrari cars sold at worldwide level

YEARS	FERRARI WORLDWIDE NUMBER OF VEHICLES (ω_i)	LINEAR TENDENCY				
		t_i	t_i^2	$t_i \omega_i$	$\omega_{t_i} = a + bt_i$	$ \omega_i - \omega_{t_i} $
2006	5671	-6	36	-34026	5769,195978	98
2007	6465	-5	25	-32325	6003,12088	462
2008	6587	-4	16	-26348	6237,219781	350

YEARS	FERRARI WORLDWIDE NUMBER OF VEHICLES (ω_i)	LINEAR TENDENCY				
		t_i	t_i^2	$t_i \omega_i$	$\omega_i = a + bt_i$	$ \omega_i - \omega_{t_i} $
2009	6250	-3	9	-18750	6471,318682	221
2010	6461	-2	4	-12922	6705,417583	244
2011	7001	-1	1	-7001	6939,516484	61
2012	7318	0	0	0	7173,615385	144
2013	6922	1	1	6922	7407,714286	486
2014	7255	2	4	14510	7641,813187	387
2015	7664	3	9	22992	7875,912088	212
2016	8014	4	16	32056	8110,010989	96
2017	8398	5	25	41990	8344,109891	54
2018	9251	6	36	55506	8578,208792	673
TOTAL	93257		182	42606	93257	3488

$$a = \frac{93257 \cdot 182 - 42606 \cdot 0}{13 \cdot 182 - 0^2} = 7173,615385; \quad b = \frac{42606}{182} = 234,0989011$$

$$v_I = \left[\frac{\sum_{i=-m}^m |\omega_i - y_{t_i}^I|}{n} : \frac{\sum_{i=-m}^m \omega_i}{n} \right] \cdot 100 = \frac{\sum_{i=-m}^m |\omega_i - \omega_{t_i}^I|}{\sum_{i=-m}^m \omega_i} \cdot 100 = \frac{3488}{93257} \cdot 100 = 3,74\%$$

- if the „sophisticated design” for ω characteristic, namely the Ferrari worldwide sales, is this mirroring $\omega_{t_i} = a + b \cdot t_i + ct_i^2$, a and b will be [3]:

$$\begin{cases} n \cdot a + b \sum_{i=1}^n t_i + c \sum_{i=1}^n t_i^2 = \sum_{i=1}^n \omega_i \\ a \sum_{i=1}^n t_i + b \cdot \sum_{i=1}^n t_i^2 + c \sum_{i=1}^n t_i^3 = \sum_{i=1}^n t_i \cdot \omega_i \\ a \cdot \sum_{i=1}^n t_i^2 + b \sum_{i=1}^n t_i^3 + c \sum_{i=1}^n t_i^4 = \sum_{i=1}^n t_i^2 \cdot \omega_i \end{cases}$$

$$a = \frac{\sum_{i=1}^n t_i^4 \sum_{i=1}^n \omega_i - \sum_{i=1}^n t_i^2 \sum_{i=1}^n t_i^2 \cdot \omega_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2}; \quad b = \frac{\sum_{i=1}^n \omega_i t_i}{\sum_{i=1}^n t_i^2}; \quad c = \frac{n \cdot \sum_{i=1}^n t_i^2 \cdot \omega_i - \sum_{i=1}^n t_i^2 \cdot \sum_{i=1}^n \omega_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2}$$

Table 6 The „conglomerate” of the statistical data which joins under the incidence of the reflection concerning the quadratic pattern for the volum of Ferrari cars sold at worldwide level

YEARS	FERRARI WORLDWIDE NUMBER OF VEHICLES (ω_i)	PARABOLIC TENDENCY					
		t_i	t_i^2	t_i^4	$t_i^2 \omega_i$	$\omega_{t_i} = a + bt_i + ct_i^2$	$ \omega_i - \omega_{t_i} $
2006	5671	-6	36	1296	204156	6107,461538	436
2007	6465	-5	25	625	161625	6172,340659	293
2008	6587	-4	16	256	105392	6267,987013	319
2009	6250	-3	9	81	56250	6394,400599	144
2010	6461	-2	4	16	25844	6551,581418	91
2011	7001	-1	1	1	7001	6739,50947	262
2012	7318	0	0	0	0	6958,244755	360
2013	6922	1	1	1	6922	7207,727272	286
2014	7255	2	4	16	29020	7487,977023	233
2015	7664	3	9	81	68976	7798,994006	135
2016	8014	4	16	256	128224	8140,778221	127
2017	8398	5	25	625	209950	8513,32967	115
2018	9251	6	36	1296	333036	8916,648351	334
TOTAL	93257		182	4550	1336396	93257	3135

$$a = \frac{\sum_{i=1}^n t_i^4 \sum_{i=1}^n \xi_i - \sum_{i=1}^n t_i^2 \sum_{i=1}^n t_i^2 \cdot \xi_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2} = \frac{4550 \cdot 93257 - 182 \cdot 1336396}{13 \cdot 4550 - 182^2} = 6958,244755$$

$$b = \frac{\sum_{i=1}^n \xi_i t_i}{\sum_{i=1}^n t_i^2} = \frac{42606}{182} = 234,0989011$$

$$c = \frac{n \cdot \sum_{i=1}^n t_i^2 \cdot \xi_i - \sum_{i=1}^n t_i^2 \cdot \sum_{i=1}^n \xi_i}{n \sum_{i=1}^n t_i^4 - \left(\sum_{i=1}^n t_i^2 \right)^2} = \frac{13 \cdot 1336396 - 182 \cdot 93257}{13 \cdot 4550 - 182^2} = 15,38361638$$

$$v_{II} = \left[\frac{\sum_{i=-m}^m |\omega_i - \omega_{t_i}''|}{n} : \frac{\sum_{i=-m}^m \omega_i}{n} \right] \cdot 100 = \frac{\sum_{i=-m}^m |\omega_i - \omega_{t_i}''|}{\sum_{i=-m}^m \omega_i} \cdot 100 = \frac{3135}{93257} \cdot 100 = 3,36\%$$

- if the „sophisticated design” for ω characteristic, namely the Ferrari worldwide sales, is this mirroring $\omega_{t_i} = ab^{t_i}$, a and b will be [3]:

$$\begin{cases} n \cdot \lg a + \lg b \cdot \sum_{i=1}^n t_i = \sum_{i=1}^n \lg \omega_i \\ \lg a \sum_{i=1}^n t_i + \lg b \cdot \sum_{i=1}^n t_i^2 = \sum_{i=1}^n t_i \cdot \lg \omega_i \end{cases}$$

$$\lg a = \frac{\left| \begin{array}{cc} \sum_{i=1}^n \lg \omega_i & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i \lg \omega_i & \sum_{i=1}^n t_i^2 \end{array} \right|}{\left| \begin{array}{cc} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{array} \right|} = \frac{\sum_{i=1}^n \lg \omega_i \sum_{i=1}^n t_i^2 - \sum_{i=1}^n t_i \lg \omega_i \sum_{i=1}^n t_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2}$$

$$\lg b = \frac{\left| \begin{array}{cc} n & \sum_{i=1}^n \lg \omega_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i \lg \omega_i \end{array} \right|}{\left| \begin{array}{cc} n & \sum_{i=1}^n t_i \\ \sum_{i=1}^n t_i & \sum_{i=1}^n t_i^2 \end{array} \right|} = \frac{n \cdot \sum_{i=1}^n t_i \lg \omega_i - \sum_{i=1}^n \lg \omega_i \sum_{i=1}^n t_i}{n \sum_{i=1}^n t_i^2 - \left(\sum_{i=1}^n t_i \right)^2}$$

Table 7 The „conglomerate” of the statistical data which joins under the incidence of the reflection concerning the exponential pattern for the volum of Ferrari cars sold at worldwide level

YEARS	FERRARI WORLDWIDE NUMBER OF VEHICLES (ω_i)	EXPONENTIAL TENDENCY				
		$\lg \omega_i$	$t_i \lg \omega_i$	$\lg \omega_{t_i} =$ $= \lg a + t_i \lg b$	$\omega_{t_i} = ab^{t_i}$	$ \omega_i - \omega_{t_i} $
2006	5671	3,753659647	-22,52195788	3,768256187	5864,840249	194
2007	6465	3,810568529	-19,05284265	3,782241521	6056,776122	408
2008	6587	3,818687663	-15,27475065	3,796226855	6254,993389	332
2009	6250	3,795880017	-11,38764005	3,810212189	6459,697619	210
2010	6461	3,810299741	-7,620599482	3,824197523	6671,101109	210
2011	7001	3,845160078	-3,845160078	3,838182857	6889,423102	112
2012	7318	3,864392405	0	3,852168191	7114,890016	203
2013	6922	3,840231595	3,840231595	3,866153525	7347,735679	426
2014	7255	3,860637417	7,621274834	3,880138859	7588,201574	333
2015	7664	3,884455960	11,65336649	3,894124193	7836,537082	173
2016	8014	3,903849338	15,61539735	3,908109527	8092,999750	79
2017	8398	3,924175870	19,62087935	3,922094861	8357,855552	40
2018	9251	3,966188681	23,79713209	3,936080195	8631,379165	620
TOTAL	93257	50,078186480	2,545330915			3340

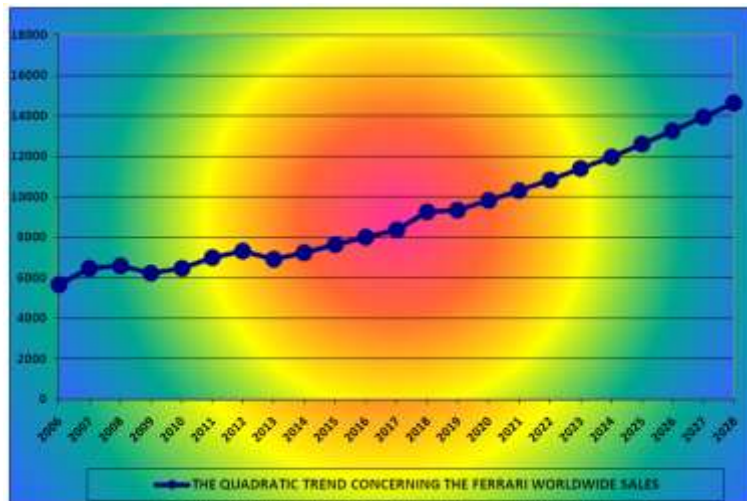
$$\lg a = \frac{50,07818648 \cdot 182 - 2,545330915 \cdot 0}{13 \cdot 182 - 0^2} = 3,85216191$$

$$\lg b = \frac{13 \cdot 2,545330915 - 50,07818648 \cdot 0}{13 \cdot 182 - 0^2} = 0,013985334$$

$$v_{\exp} = \left[\frac{\sum_{i=-m}^m |\omega_i - \omega_{t_i}^{\exp}|}{n} : \frac{\sum_{i=-m}^m \omega_i}{n} \right] \cdot 100 = \frac{\sum_{i=-m}^m |\omega_i - \omega_{t_i}^{\exp}|}{\sum_{i=-m}^m \omega_i} \cdot 100 = \frac{3340}{93257} \cdot 100 = 3,58\%$$

$$v_{II} = 3,36\% < v_{\exp} = 3,58\% < v_I = 3,74\%$$

The „design of the rally” concerning the projection for ω factor, which belongs to the Ferrari worldwide sales, is a quadratic pattern $\omega_{t_i} = a + b \cdot t_i + ct_i^2$



Graph 2 The design of the quadratic pattern regarding the worldwide sales for the Ferrari cars

Because the design of the modelling for the values of Lamborghini and Ferrari cars sold at worldwide level shows a quadratic pattern $\xi_{t_i} = a + b \cdot t_i + ct_i^2$, the forecasts projected will be:

$$\begin{aligned}
 \xi_{2019}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 7 + 56,41258741 \cdot 7^2 = 6204,517482 \approx 6204 \text{ vehicles} \\
 \xi_{2020}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 8 + 56,41258741 \cdot 8^2 = 7277,607392 \approx 7277 \text{ vehicles} \\
 \xi_{2021}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 9 + 56,41258741 \cdot 9^2 = 8463,522477 \approx 8463 \text{ vehicles} \\
 \xi_{2022}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 10 + 56,41258741 \cdot 10^2 = 9762,262737 \approx 9762 \text{ vehicles} \\
 \xi_{2023}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 11 + 56,41258741 \cdot 11^2 = 11173,82817 \approx 11174 \text{ vehicles} \\
 \xi_{2024}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 12 + 56,41258741 \cdot 12^2 = 12698,21878 \approx 12698 \text{ vehicles} \\
 \xi_{2025}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 13 + 56,41258741 \cdot 13^2 = 14335,43457 \approx 14335 \text{ vehicles} \\
 \xi_{2026}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 14 + 56,41258741 \cdot 14^2 = 16085,47552 \approx 16085 \text{ vehicles} \\
 \xi_{2027}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 15 + 56,41258741 \cdot 15^2 = 17948,34166 \approx 17948 \text{ vehicles} \\
 \xi_{2028}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 16 + 56,41258741 \cdot 16^2 = 19924,63297 \approx 19924 \text{ vehicles} \\
 \xi_{2029}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 17 + 56,41258741 \cdot 17^2 = 22012,54945 \approx 22012 \text{ vehicles} \\
 \xi_{2030}^{LAMBORGHINI} &= 185,993007 + 226,9010989 \cdot 18 + 56,41258741 \cdot 18^2 = 24213,89111 \approx 24214 \text{ vehicles} \\
 \omega_{2019}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 7 + 15,38361638 \cdot 7^2 = 9350,734265 \approx 9351 \text{ vehicles} \\
 \omega_{2020}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 8 + 15,38361638 \cdot 8^2 = 9815,587412 \approx 9816 \text{ vehicles} \\
 \omega_{2021}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 9 + 15,38361638 \cdot 9^2 = 10311,20779 \approx 10311 \text{ vehicles} \\
 \omega_{2022}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 10 + 15,38361638 \cdot 10^2 = 10837,5954 \approx 10838 \text{ vehicles} \\
 \omega_{2023}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 11 + 15,38361638 \cdot 11^2 = 11394,75025 \approx 11395 \text{ vehicles} \\
 \omega_{2024}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 12 + 15,38361638 \cdot 12^2 = 11982,67233 \approx 11983 \text{ vehicles} \\
 \omega_{2025}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 13 + 15,38361638 \cdot 13^2 = 12601,36164 \approx 12601 \text{ vehicles} \\
 \omega_{2026}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 14 + 15,38361638 \cdot 14^2 = 13250,81818 \approx 13251 \text{ vehicles} \\
 \omega_{2027}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 15 + 15,38361638 \cdot 15^2 = 13931,04196 \approx 13931 \text{ vehicles} \\
 \omega_{2028}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 16 + 15,38361638 \cdot 16^2 = 14642,03297 \approx 14642 \text{ vehicles} \\
 \omega_{2029}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 17 + 15,38361638 \cdot 17^2 = 15383,79121 \approx 15384 \text{ vehicles} \\
 \omega_{2030}^{FERRARI} &= 6958,244755 + 234,0989011 \cdot 18 + 15,38361638 \cdot 18^2 = 16156,31668 \approx 16156 \text{ vehicles}
 \end{aligned}$$

Table 8 Statistical pol position leadership between Lamborghini & Ferrari, in the period 2006-2030

YEARS	LAMBORGHINI WORLDWIDE NUMBER OF VEHICLES	FERRARI WORLDWIDE NUMBER OF VEHICLES	THE DYNAMICS CONCERNING THE LEADERSHIP					
			$I_{Ferrari / Lamb}^{CARS}$	$I_{Lambo / Ferrari}^{CARS}$	(RELATIVE RISES) (%)		$\Delta_{Ferrari / Lamb}^{CARS}$	$\Delta_{Lambo / Ferrari}^{CARS}$
							(ABSOLUTE RISES) (NUMBER OF VEHICLES)	
2006	2087	5671	271,73		171,73		3584	
2007	2406	6465	268,70		168,70		4059	
2008	2430	6587	271,07		171,07		4157	
2009	1515	6250	412,54		312,54		4735	
2010	1302	6461	496,24		396,24		5159	
2011	1602	7001	437,02		337,02		5399	
2012	2083	7318	352,32		252,32		5235	
2013	2121	6922	326,36		226,36		4801	
2014	2530	7255	286,76		186,76		4725	
2015	3245	7664	236,18		136,18		4419	
2016	3457	8014	231,82		131,82		4557	
2017	3815	8398	220,13		120,13		4583	
2018	5750	9251	160,89		60,89		3501	
2019	6244	9351	149,76		49,76		3107	
2020	7277	9816	134,89		34,89		2539	
2021	8463	10311	121,84		21,84		1848	
2022	9762	10838	111,02		11,02		1076	
2023	11174	11395	101,98		1,98		221	
2024	12698	11983		105,97		5,97		715
2025	14335	12601		113,76		13,76		1734
2026	16085	13251		121,39		21,39		2834
2027	17948	13931		128,83		28,83		4017
2028	19924	14642		136,07		36,07		5282
2029	22012	15384		143,08		43,08		6628
2030	24214	16156		149,88		49,88		8058

5. Conclusions

The profile of the pattern which paints the values of the worldwide sales regarding the Lamborghini cars, between 2006-2018, unveils a propensity to the quadratic representation. The configuration of the design which is projected on the volum of the worldwide sales concerning the Ferrari cars, between 2006-2018, reveals a proclivity to the quadratic tendency. We can see that in 2018, Ferrari had a rise with 60,89 %, comparative to Lamborghini, of the value concerning the number of cars sold in the worldwide sphere. Also, in 2024 Lamborghini will obtain a rise with 5,97 % comparative to Ferrari, of the value regarding the number of cars sold at the worldwide plan. If we analysis the forecasts regarding the number of cars sold at the worldwide level, in 2030 Lamborghini will achieve a growth with 49,88% comparative to Ferrari. So, we can say that, there is a strong meeting in pol position concerning the leadership between these two great „hypersonic” leaders and this competition will be forever with effects on the adrenalin for the lovers of super exotic cars.

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